

1. (20%) A 0.2-kg ball is thrown from the ground with the initial velocity \bar{v}_0 as shown in Fig 1.

In addition to its weight, there is a constant wind force of 8 newtons acting in the y direction. Please find (a) (10%) the position of the ball at the instant it returns to the elevation from which it was thrown, and (b) (10%) the velocity of the ball at that instant.

Note: (i) Use g (gravitational acceleration) = 9.81 m/s^2 .

(ii) $\sqrt{2} = 1.414$.

(iii) Please use the vector form to express the answers (position and velocity); e.g. $\bar{r} = a\bar{i} + b\bar{j} + c\bar{k}$, where a , b , and c are the calculated results; \bar{i} , \bar{j} , and \bar{k} are the unit vectors along the x-, y-, and z- directions, respectively.

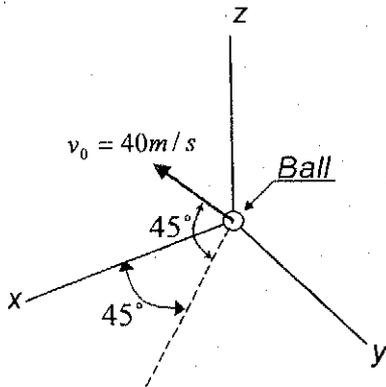


Fig. 1

2. (20%) Two steel balls, each of mass m , are welded to a light rod of length L and negligible mass and are initially at rest on a smooth horizontal surface. A horizontal force of magnitude F is suddenly applied to the rod as shown in Fig. 2. Please determine

(a) (10%) the instantaneous acceleration \bar{a} of the mass center G .

(b) (10%) the corresponding rate $\dot{\theta}$ at which the angular velocity of the assembly about G is changing with time.

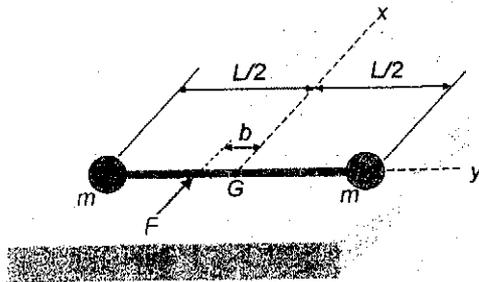


Fig. 2

3. (30%) Two spheres of uniform density, A and B, start from rest and roll, without slipping, down the same incline (Fig. 3). If the radius of Sphere A is larger than that of Sphere B, then
- (10%) which sphere gets to the bottom first?
 - (20%) Explain your answer to (a).

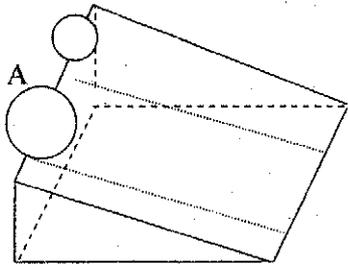


Fig. 3

4. (15%) Given a rigid body in the three-dimensional space, please answer the following questions.
- (5%) How many principal axes does the rigid body possess? What are the differences between these principal axes?
 - (10%) Suppose that we want to rotate the rigid body with respect to a fixed axis at a constant angular velocity. Which axis (relative to the rigid body) will yield the minimum rotational energy? Why?
5. (15%) A simplified model for the suspension of a car is shown in Fig. 4, where m is the total mass of the car and k is the effective stiffness. The car is moving along a bumpy road with bumps equally separated by a distance d . Please find the velocity of the car, v , that will result in largest vibration in the vertical direction.

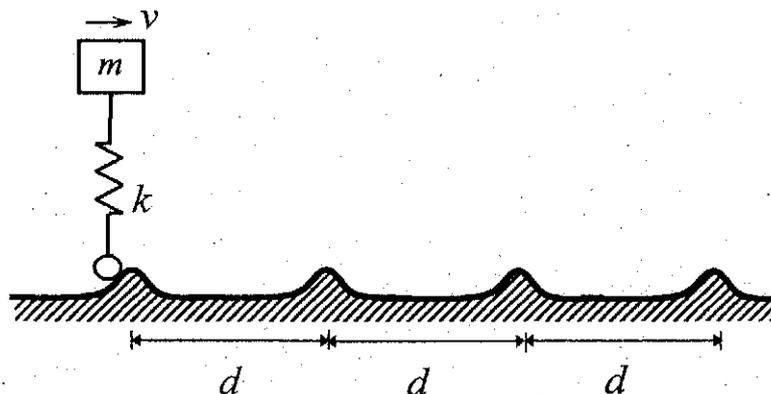


Fig. 4