

1. (10%) Consider a unity-feedback control system as shown in Fig. 1 with a plant transfer function $G(s) = \frac{15}{s(s+2)(s+50)}$ and a proportional controller K_P . Determine (i) the range of K_P for closed-loop stability by applying the Routh criterion, (ii) the type of the unity-feedback system and (iii) its corresponding steady-state tracking error for a unit-step command, i.e., $y^*(t) = 1$.

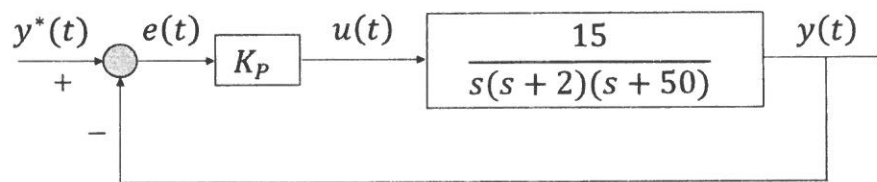


Fig. 1

2. (20%) Consider another feedback control system as shown in Fig. 2 with $K_P = 10$.

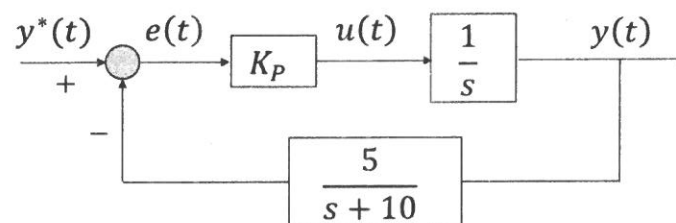


Fig. 2

- (a) (5%) Determine steady-state tracking error $\lim_{t \rightarrow \infty} (y^*(t) - y(t))$ for a unit-step command $y^*(t) = 1$.
- (b) (10%) Estimate its transient performance in terms of every applicable performance index such as the time constant, rise time, peak time, %OV, and/or settling time.
- (c) (5%) It can be shown that there is a zero in the close-loop transfer function. What will this extra zero affect your estimate of the transient performance in (b)?

3. (20%) Consider the following dynamic system of a permanent magnetic DC motor where $K_m = 2 \frac{V}{\text{rad/s}} = 2 \frac{N.m}{A}$ is the motor constant, $L = 0.012 H, R = 0.6 \Omega, J = 12 \text{ kg.m}^2, B = 10 \frac{N.m}{\text{rad/s}}$ are the inductance and resistance of the motor coil and the inertia and viscous damping coefficient of the rotational load, respectively. When a motor voltage v is applied, the coil current i and motor speed ω change.

$$L \frac{di}{dt} + Ri = v - K_m \omega$$

$$J \frac{d\omega}{dt} = K_m i - B\omega$$

- (a) (5%) Determine the transfer function from the input voltage v to the output motor speed ω .
- (b) (5%) (i) Can we apply the final-value theorem of the Laplace transform to determine the steady-state motor speed ω_{ss} when a unit-step command voltage v is applied and why? (ii) If can, calculate the steady-state speed ω_{ss} when $v = 1 \text{ V}$.
- (c) (10%) (i) Show that the system is a dominantly 1st-order system. That is the dynamic response of the system can be approximated as that of a first order system. (ii) Then, what is the transfer function of the approximate 1st order system? (iii) What is the approximate time constant? (iv) Will the actual time constant be faster or slower than the approximate time constant and why?
4. (25%) Given the unit-feedback system with

$$G(s) = \frac{K}{s(s+3)(s+9)}$$

Plot the root locus and find the breakaway points, asymptotes.

5. (25%) (a) (15%) Sketch the Bode asymptotic magnitude and phase plots for the function.

$$G(s) = \frac{10(s+10)}{(s+1)(s^2+10s+25)}$$

- (b) (10%) Find the approximate gain margin and phase margin using the Bode plot in (a).