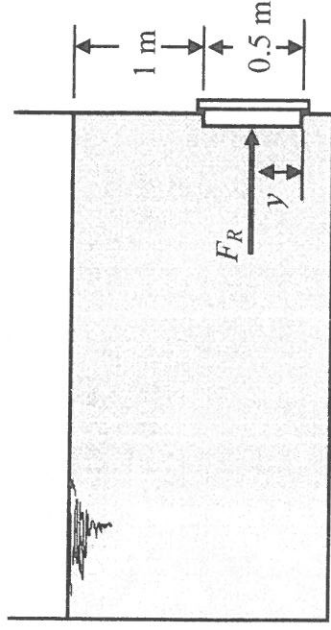


(15%)

1. A water tank has a square  $0.5 \times 0.5 \text{ m}^2$  plate bolted to one side of its wall. Determine the magnitude  $F_R$  and location  $y$  of the resultant force on the attached plate. (Specific weight of water is  $10 \text{ kN/m}^3$ )



(10%)

2. The velocity field of an incompressible, steady flow is given by  $\vec{V}(u, v, w) = u\vec{i} + v\vec{j} + w\vec{k}$ ,

where

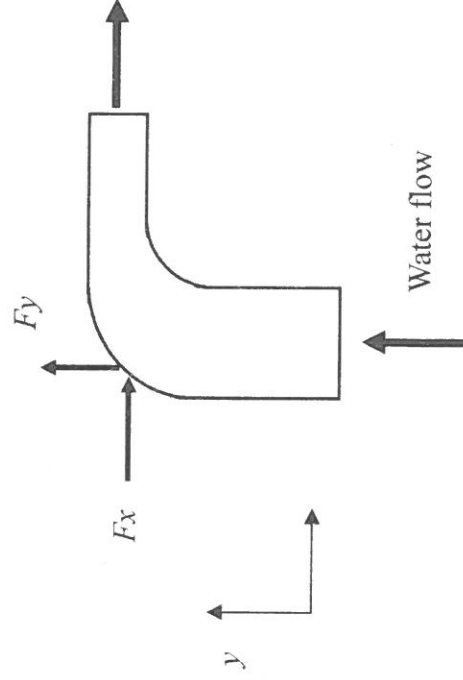
$$u = x^2 - y^2 + z$$

$$v = x - zy - z^2$$

Determine the form of the  $z$  component,  $w$ , required to satisfy the continuity equation.

(25%)

3. Water flows through a horizontal,  $90^\circ$  pipe bend as shown in the figure. The cross-sectional areas of the pipe inlet and outlet are  $20 \text{ cm}^2$  and  $6 \text{ cm}^2$ , respectively. The absolute pressure at the entrance is  $150 \text{ kPa}$ . The flow velocity of the water is  $10 \text{ m/s}$  when it exits the pipe. Calculate the horizontal components of the anchoring force required to hold the pipe in place. (Ambient pressure is  $100 \text{ kPa}$ . Water density is  $1000 \text{ kg/m}^3$ )

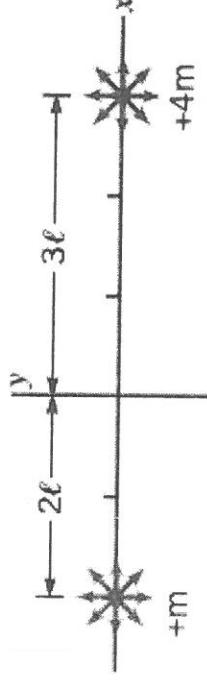


(20%)

4. The drag on a 2 m diameter satellite dish due to a 100 km/h wind is to be determined through a wind tunnel test using a geometry similar 0.4 m diameter model dish. Assume standard air for both model and prototype and the drag ( $D$ ) is a function of the diameter of the dish ( $d$ ), the speed of the air ( $v$ ), the viscosity of the air ( $\mu$ ), the density of the air ( $\rho$ ).
- (a) Please determine a suitable set of dimensionless variables for this problem, the drag being the independent variable. (10%)
- (b) What air speed should the model test be run. (5%)
- (c) With all similarity conditions satisfied, the measured drag on the model was determined to be 200 N. What is the predicted drag on the prototype dish? (5%)

(15%)

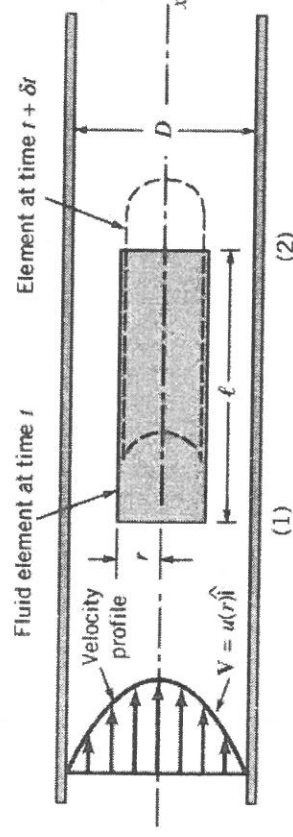
5. Two sources, one of strength  $m$  and the other with strength  $4m$ , are located on the  $x$  axis as shown below. Determine the location of the stagnation point the flow produced by these sources.



(15%)

6. For a fully developed laminar flow in a pipe (Hagen-Poiseuille flow), shown below. Please show that the pressure drop can be calculated as a function of the length of the fluid element, the shear stress at the wall and the diameter of the pipe as shown in the following equation.

$$\Delta p = \frac{4l\tau_w}{D}$$



Supplementary information

■ TABLE 6.1  
Summary of Basic, Plane Potential Flows.

Description of Flow Field	Velocity Potential	Stream Function	Velocity Components <sup>a</sup>
Uniform flow at angle $\alpha$ with the $x$ axis (see Fig. 6.16b)	$\phi = U(x \cos \alpha + y \sin \alpha)$	$\psi = U(y \cos \alpha - x \sin \alpha)$	$u = U \cos \alpha$ $v = U \sin \alpha$
Source or sink (see Fig. 6.17) $m > 0$ source $m < 0$ sink	$\phi = \frac{m}{2\pi} \ln r$	$\psi = \frac{m}{2\pi} \theta$	$v_r = \frac{m}{2\pi r}$ $v_\theta = 0$
Free vortex (see Fig. 6.18) $\Gamma > 0$ counterclockwise motion $\Gamma < 0$ clockwise motion	$\phi = \frac{\Gamma}{2\pi} \theta$	$\psi = -\frac{\Gamma}{2\pi} \ln r$	$v_r = 0$ $v_\theta = \frac{\Gamma}{2\pi r}$
Doublet (see Fig. 6.23)	$\phi = \frac{K \cos \theta}{r}$	$\psi = -\frac{K \sin \theta}{r}$	$v_r = -\frac{K \cos \theta}{r^2}$ $v_\theta = -\frac{K \sin \theta}{r^2}$

<sup>a</sup>Velocity components are related to the velocity potential and stream function through the relationships:

$$u = \frac{\partial \phi}{\partial x} = \frac{\partial \psi}{\partial y} \quad v = \frac{\partial \phi}{\partial y} = -\frac{\partial \psi}{\partial x} \quad v_r = \frac{1}{r} \frac{\partial \phi}{\partial r} = \frac{1}{r} \frac{\partial \psi}{\partial \theta} = -\frac{\partial \psi}{\partial r} \quad v_\theta = \frac{1}{r} \frac{\partial \phi}{\partial \theta} = -\frac{\partial \phi}{\partial r}$$